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AND ALUMINUM FLUORIDES WITH A FLUORIDE-SELECTIVE ELECTRODE

by

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DETERMINATION OF STABILITY CONSTANTS OF HYDROGEN  
AND ALUMINUM FLUORIDES WITH A FLUORIDE-SELECTIVE ELECTRODE\*

by

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Abstract—Stability quotients for the hydrogen-fluoride and aluminum-fluoride systems in  $\text{NH}_4\text{NO}_3$  were determined from measurements of free fluoride ion concentration by the lanthanum fluoride membrane electrode. Stability quotients at 0.5, 0.3, 0.1, and 0.01 M ionic strength were extrapolated to infinite dilution through the Debye-Hückel equation to obtain thermodynamic stability constants at 25°C for  $\text{HF}$ ,  $\text{HF}_2^-$ ,  $\text{AlF}_2^+$ ,  $\text{AlF}_3$ , and  $\text{AlF}_4^-$ .

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## INTRODUCTION

The lanthanum fluoride membrane electrode[1], which responds specifically and theoretically to changes of fluoride ion activity in solution, is a new tool for potentiometric investigation of metal-fluoride complexes[2,3]. An earlier fluoride-responsive electrode, the reversible lead amalgam-lead fluoride electrode, was used by Broene and DeVries[4] to investigate the hydrogen-fluoride system. Uncomplexed fluoride has also been determined indirectly from changes in hydrogen ion concentration or from potential changes in the ferrous-ferric couple[5].

The ability to directly determine free fluoride ion concentration (or mean activity) simplifies gathering and interpretation of experimental data for studies of metal complexes. In this work, the new lanthanum fluoride electrode was used to measure free fluoride ion in an investigation of the hydrogen-fluoride and aluminum-fluoride systems in  $\text{NH}_4\text{NO}_3$ . Stability quotients obtained at 0.5 M corroborate the classic work of Brosset and Orring[5]. Additional data at ionic strengths down to 0.01 M were extrapolated to infinite dilution to obtain thermodynamic stability constants.

1. M. S. Frant and J. W. Ross, Jr., Science **154**, 1553 (1966).
2. K. Srinivasan and G. A. Rechnitz, Anal. Chem. **40**, 509 (1968).
3. R. E. Mesmer and C. F. Baes, Jr., Beryllium Fluoride Complexes in 1 M NaCl and 1 M NaClO<sub>4</sub>. 156th American Chemical Society National Meeting, September 1968.
4. H. H. Broene and T. DeVries, J. Am. Chem. Soc. **69**, 1644 (1947).
5. C. Brosset and J. Orring, Svensk Kem. Tidskr. **55**, 101 (1943).

## EXPERIMENTAL

Reagent-grade chemicals were used. Solutions were made in deionized water. Glass volumetric ware was used to prepare solutions, but solutions were stored in polyethylene to avoid prolonged contact with glass.

Standard NaF solutions were prepared from NaF that was dried several hours at 120°C. HF and HNO<sub>3</sub> were standardized by titration to pH 7 with standard NaOH. NH<sub>4</sub>F was prepared by precise neutralization of the standardized HF with NH<sub>4</sub>OH. Al(NO<sub>3</sub>)<sub>3</sub> solutions were standardized by titrating the acid displaced by a measured volume passed through a column of "Amberlite"\* IR-120 in the hydrogen form.

The experimental solutions were determinate mixtures, equilibrated in a water bath at 25±0.1°C, of acid (HF or HNO<sub>3</sub>) and fluoride (HF or NH<sub>4</sub>F), plus Al(NO<sub>3</sub>)<sub>3</sub> in the fluoroaluminate investigation. Ionic strengths of 0.5, 0.3, 0.1, or 0.01 M were maintained constant with NH<sub>4</sub>NO<sub>3</sub>. During measurement, the 50-ml solutions were stirred in polypropylene beakers with "Teflon"\*\*-coated magnetic stirring bars. In some cases a single solution was used for a single measurement, but in other cases, data were generated by titration of the initial solution with fluoride or aluminum.

The fluoride indicator electrode (Orion\*\*\* 94-09) was used with a saturated calomel reference electrode (Beckman\*\*\*\* 39170) that was protected from fluoride by a paraffin coating, save for the fiber

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\*\*\* Orion Research Incorporated, Cambridge, Mass.

\*\*\*\* Beckman Instruments, Inc., Fullerton, California

junction at the tip. Potentials were measured to  $\pm 0.1$  mV with an Orion digital pH Meter, Model 801.

The electrodes were calibrated daily in standard solutions of fluoride ( $\text{NH}_4\text{F}$  or  $\text{NaF}$ ) in the concentration range and at the ionic strength in  $\text{NH}_4\text{NO}_3$  of the experiments. Experimental concentrations were calculated by the Nernst equation, which was obeyed over the range of concentrations used.

#### INTERPRETATION OF DATA

The experimental results were interpreted according to the Bjerrum formulation[6] in terms of  $\bar{n}$ , defined as the average number of fluoride ligands bound per complexing atom. This  $\bar{n}$  can be expressed as a function of the free fluoride ion concentration,  $F$ , and the stability quotients,  $k_n$ , of the successively formed fluoride complexes with the atom  $M^{x+}$ :

$$\bar{n} = \frac{k_1 F + 2k_1 k_2 F^2 + \dots + nk_1 k_2 \dots k_n F^n}{1 + k_1 F + k_1 k_2 F^2 + \dots + k_1 k_2 \dots k_n F^n} \quad (1)$$

The stability quotient,  $k_n$ , is given in terms of the concentrations of the equilibrium components:

$$k_n = \frac{[(MF_n)^{x-n}]}{[(MF_{n-1})^{x-n-1}][F^-]} \quad (2)$$

For the hydrogen system,  $\bar{n}$  was calculated from the total fluoride and hydrogen ions added,  $F_T$  and  $H_T$ , and the measured free fluoride ion concentration,  $F$ :

6. J. Bjerrum, Metal Ammine Formation in Aqueous Solution. Theory of the Reversible Step Reactions, P. Haase and Son, Copenhagen (1941).

$$\bar{n}_H = \frac{F_T - F}{H_T} = \frac{(HF) + 2(HF_2^-)}{H_T} \quad (3)$$

Stability quotients were calculated by fitting the experimental  $\bar{n}$  and  $F$  values to Equation (1), as described below.

For the aluminum-fluoride system, which includes the hydrogen-fluoride equilibria,  $\bar{n}_{Al}$  was calculated by

$$\bar{n}_{Al} = \frac{F_T - F - (HF) - 2(HF_2^-)}{Al_T} \quad (4)$$

$$= \frac{F_T - F - \bar{n}_H H_T}{Al_T} \quad (4a)$$

Values of  $\bar{n}_H$  were calculated by Equation (1) for each experimental  $F$  using stability quotients determined for the hydrogen-fluoride system at the same ionic strength.

The experimental data were fitted by computer to Equation (1), using a method that numerically determines local minima of positive-valued differentiable functions of several variables[7]. Estimates were made for each set of stability quotients,  $\prod_{n=1}^n k_n$ , which were used for computation of the final values. The range of experimental data was not sufficient to define  $k_5$  and  $k_6$  experimentally; therefore the reasonable values of 30 and 3, were chosen for  $k_5$  and  $k_6$  to establish this end of the curve and improve the accuracy of the calculated  $k_4$ .

[7] W. C. Davidon, Variable Metric Method for Minimization.  
Argonne National Laboratory Report No. ANL 5990, (1959).

## RESULTS AND DISCUSSION

Stability Quotients

Bjerrum formation curves for the hydrogen-fluoride and aluminum-fluoride systems in 0.5, 0.3, 0.1, and 0.01 M  $\text{NH}_4\text{NO}_3$  are presented in Figures 1 and 2, where the ordinates have been individualized to avoid overlap of the curves. The fitted curve is drawn through each set of data. The fit was evaluated through the  $\bar{n}$  residuals; the standard deviation was 0.05 or below for every curve, and the sum of the residuals was always less than 0.1, indicating that the fit was satisfactory.

Experimental data in Tables 1 and 2 illustrate the concentration ranges of the several components.

Computed stability quotients are given in Tables 3 and 4, where they are compared with those obtained by Brosset in 0.53 M  $\text{NH}_4\text{NO}_3$ . On the basis of the known experimental errors and the fitting of the curves, relative precisions of these quotients are estimated to be 5 to 10%.

Experimental results were not consistent at higher fluoride concentrations, for definition of  $k_3$  and  $k_5$ . Fluoride values were sometimes high, suggesting that  $\text{HF}_2^-$  may interfere with electrode response, but this could not be demonstrated conclusively. In the complicated fluoroaluminate system, the formation of species other than those postulated could also have caused the irregularities.



Stability Constants

The stability quotients obtained at the four ionic strengths provide the basis for calculation of thermodynamic stability constants ( $K_n$ ) in both the hydrogen-fluoride and aluminum-fluoride systems by extrapolation to infinite dilution. The Debye-Huckel equation was used, with 1.5 as a reasonable factor to account for the ion size parameter. The fitting was done through the constant C of the linear term.

$$\log K_n = \log k_n - \frac{\Delta Z_n^2 (0.511) \sqrt{\mu}}{1 + 1.5 \sqrt{\mu}} + C\mu \quad (5)$$

where

$$\Delta Z_n^2 = \sum (\text{charge})^2_{\text{products}} - \sum (\text{charge})^2_{\text{reactants}} \quad (6)$$

which comes from the Debye-Hückel formulation; for example, in the aluminum system,  $\Delta Z_1^2 = -6$ .

Results are given in Tables 5 and 6, together with published stability constants. The stability constants in the hydrogen system were determined directly by Broene and DeVries[4]. Those of the aluminum system are Brosset's[5] data converted to infinite dilution by numerical corrections used by Paul[9] for other polyvalent metal fluoride complexes. The present extrapolations agree remarkably well with the published values. The fact that the experimental data at the four ionic strengths fall into the proper sequence for extrapolation by the Debye-Hückel equation lends validity to these measurements by the lanthanum fluoride electrode.

9. A. D. Paul. University of California Radiation Laboratory Report No. UCRL 2926, (1955).

Acknowledgement—The help of W. L. Fillinger, who furnished the basic computer program and adapted it to our needs, is gratefully acknowledged.

Table 1. Experimental Data: Hydrogen-Fluoride System

| <u>Concentration (mM)</u>                    |                      |          |                             |
|--|----------------------|----------|-----------------------------|
| <u>F<sub>T</sub></u>                         | <u>H<sub>T</sub></u> | <u>F</u> | <u><math>\bar{n}</math></u> |
| <u>In 0.5 M NH<sub>4</sub>NO<sub>3</sub></u> |                      |          |                             |
| 0.9784                                       | 9.902                | 0.137    | 0.085                       |
| 1.953  | 9.883                | 0.295    | 0.168                       |
| 4.761  | 19.630               | 0.422    | 0.221                       |
| 5.000  | 20.612               | 0.417    | 0.223                       |
| 5.000  | 20.612               | 0.409    | 0.223                       |
| 2.924  | 9.863                | 0.475    | 0.248                       |
| 3.891  | 9.844                | 0.680    | 0.326                       |
| 4.854  | 9.825                | 0.930    | 0.399                       |
| 4.854  | 9.825                | 0.900    | 0.402                       |
| 9.433  | 19.445               | 1.109    | 0.428                       |
| 10.00  | 20.612               | 1.080    | 0.433                       |
| 5.335  | 9.816                | 1.070    | 0.434                       |
| 5.814  | 9.806                | 1.220    | 0.468                       |
| 6.292  | 9.797                | 1.410    | 0.498                       |
| 6.770  | 9.788                | 1.580    | 0.530                       |
| 7.722  | 9.768                | 2.000    | 0.586                       |
| 8.670  | 9.749                | 2.450    | 0.638                       |
| 9.615  | 9.731                | 2.950    | 0.685                       |
| 9.615  | 9.731                | 2.800    | 0.700                       |
| 18.518                                       | 19.085               | 4.091    | 0.756                       |
| 20.00  | 20.612               | 4.170    | 0.768                       |
| 20.00  | 20.612               | 4.100    | 0.771                       |
| 24.93  | 22.14                | 6.559    | 0.830                       |
| 27.272                                       | 18.738               | 10.271   | 0.907                       |
| <u>In 0.3 M NH<sub>4</sub>NO<sub>3</sub></u> |                      |          |                             |
| 0.294  | 5.876                | 0.0320   | 0.045                       |
| 0.587  | 5.871                | 0.119    | 0.080                       |
| 0.590  | 4.420                | 0.151    | 0.099                       |
| 1.172  | 5.859                | 0.253    | 0.157                       |
| 0.597  | 0.994                | 0.381    | 0.217                       |
| 0.597  | 0.829                | 0.411    | 0.224                       |
| 1.754  | 5.848                | 0.403    | 0.231                       |
| 0.597  | 0.664                | 0.440    | 0.236                       |
| 0.598  | 0.504                | 0.472    | 0.250                       |
| 0.598  | 0.339                | 0.511    | 0.257                       |
| 2.335  | 5.836                | 0.577    | 0.301                       |

Table 1. (Continued)

| <u>Concentration (mM)</u> |                      |          |                             |
|---------------------------|----------------------|----------|-----------------------------|
| <u>F<sub>T</sub></u>      | <u>H<sub>T</sub></u> | <u>F</u> | <u><math>\bar{n}</math></u> |
| 1.478                     | 2.96                 | 0.586    | 0.301                       |
| 2.913                     | 5.825                | 0.773    | 0.367                       |
| 2.913                     | 5.82                 | 0.768    | 0.369                       |
| 3.488                     | 5.814                | 1.003    | 0.427                       |
| 4.062                     | 5.803                | 1.257    | 0.483                       |
| 2.941                     | 2.941                | 1.429    | 0.514                       |
| 4.633                     | 5.792                | 1.533    | 0.535                       |
| 5.202                     | 5.780                | 1.812    | 0.586                       |
| 5.769                     | 5.769                | 2.176    | 0.623                       |
| 5.77                      | 5.77                 | 2.162    | 0.625                       |
| 4.390                     | 2.927                | 2.494    | 0.648                       |
| 7.177                     | 5.742                | 3.150    | 0.701                       |
| 5.825                     | 2.912                | 3.693    | 0.732                       |
| 8.571                     | 5.714                | 4.185    | 0.768                       |
| 9.953                     | 5.687                | 5.325    | 0.814                       |
| 8.654                     | 2.885                | 6.249    | 0.834                       |
| 25.21                     | 22.69                | 6.090    | 0.843                       |
| 11.32                     | 5.66                 | 6.533    | 0.846                       |
| 11.32                     | 5.660                | 6.522    | 0.847                       |
| 25.64                     | 17.95                | 9.500    | 0.899                       |
| 16.67                     | 5.56                 | 11.57    | 0.917                       |
| 26.09                     | 13.04                | 13.76    | 0.946                       |
| 16.822                    | 2.804                | 14.10    | 0.971                       |
| 26.79                     | 5.357                | 21.02    | 1.077                       |

In 0.1 M NH<sub>4</sub>NO<sub>3</sub>

|        |        |        |       |
|--------|--------|--------|-------|
| 0.0706 | 0.0706 | 0.0699 | 0.053 |
| 0.0940 | 0.0940 | 0.0872 | 0.072 |
| 0.1904 | 0.0906 | 0.178  | 0.132 |
| 0.232  | 0.232  | 0.195  | 0.160 |
| 0.289  | 0.289  | 0.234  | 0.189 |
| 0.400  | 0.400  | 0.310  | 0.224 |
| 0.509  | 0.509  | 0.377  | 0.261 |
| 1.183  | 2.959  | 0.390  | 0.268 |
| 0.720  | 0.720  | 0.503  | 0.302 |
| 0.998  | 0.998  | 0.669  | 0.329 |
| 1.772  | 2.953  | 0.650  | 0.380 |
| 1.342  | 1.342  | 0.797  | 0.406 |
| 1.780  | 1.780  | 0.968  | 0.456 |

Table 1. (Continued)

| <u>Concentration (mM)</u> |                      |          |                             |
|---------------------------|----------------------|----------|-----------------------------|
| <u>F<sub>T</sub></u>      | <u>H<sub>T</sub></u> | <u>F</u> | <u><math>\bar{n}</math></u> |
| 2.358                     | 2.947                | 0.960    | 0.474                       |
| 1.993                     | 1.993                | 1.046    | 0.475                       |

In 0.01 M NH<sub>4</sub>NO<sub>3</sub>

|        |        |        |       |
|--------|--------|--------|-------|
| 0.0921 | 0.6004 | 0.0543 | 0.063 |
| 0.1838 | 1.199  | 0.0796 | 0.087 |
| 0.1840 | 0.6919 | 0.1044 | 0.115 |
| 0.1988 | 0.1988 | 0.1671 | 0.160 |
| 0.3668 | 1.3797 | 0.1531 | 0.155 |
| 0.3972 | 1.518  | 0.1568 | 0.158 |
| 0.2754 | 0.7831 | 0.1506 | 0.159 |
| 0.2136 | 0.2136 | 0.1755 | 0.178 |
| 0.3976 | 1.013  | 0.2014 | 0.194 |
| 0.3672 | 0.8742 | 0.1940 | 0.198 |
| 0.5491 | 1.560  | 0.2218 | 0.210 |
| 0.4585 | 0.9650 | 0.2347 | 0.232 |
| 0.3980 | 0.5070 | 0.2763 | 0.240 |
| 0.7307 | 1.7396 | 0.2872 | 0.255 |
| 0.4263 | 0.4263 | 0.3063 | 0.281 |
| 0.5502 | 0.5502 | 0.3830 | 0.304 |
| 0.6382 | 0.6382 | 0.4182 | 0.345 |
| 0.8492 | 0.8492 | 0.5140 | 0.395 |
| 1.059  | 1.059  | 0.6025 | 0.431 |
| 1.477  | 1.477  | 0.7580 | 0.487 |
| 1.892  | 1.892  | 0.8926 | 0.528 |

Table 2. Experimental Data: Aluminum-Fluoride System

| Concentration (mM)  |        |        |         |           |
|---------------------|--------|--------|---------|-----------|
| $R_T$               | $H_T$  | Al     | F       | $\bar{n}$ |
| In 0.5 M $NH_4NO_3$ |        |        |         |           |
| 9.174               | 4.760  | 13.762 | 0.00112 | 0.666     |
| 1.000               | 5.153  | 1.250  | 0.00200 | 0.793     |
| 9.259               | 4.804  | 11.574 | 0.00152 | 0.799     |
| 9.259               | 4.804  | 11.574 | 0.00180 | 0.799     |
| 4.900               | 19.908 | 4.902  | 0.00360 | 0.989     |
| 9.345               | 4.848  | 9.345  | 0.00276 | 0.999     |
| 9.416               | 4.885  | 7.533  | 0.00544 | 1.247     |
| 9.469               | 4.913  | 6.155  | 0.01189 | 1.530     |
| 9.505               | 4.931  | 5.228  | 0.02510 | 1.797     |
| 2.500               | 5.153  | 1.250  | 0.03640 | 1.870     |
| 9.525               | 4.942  | 4.762  | 0.04117 | 1.963     |
| 9.525               | 4.942  | 4.762  | 0.04247 | 1.962     |
| 9.540               | 4.949  | 4.293  | 0.0758  | 2.147     |
| 9.560               | 4.960  | 3.824  | 0.1360  | 2.353     |
| 9.578               | 4.969  | 3.352  | 0.2448  | 2.569     |
| 5.000               | 5.153  | 1.250  | 0.4430  | 2.675     |
| 18.182              | 18.867 | 4.546  | 0.5340  | 2.757     |
| 9.597               | 4.979  | 2.879  | 0.4373  | 2.778     |
| 41.667              | 17.293 | 12.500 | 0.5690  | 2.895     |
| 20.361              | 18.878 | 4.525  | 0.7379  | 2.918     |
| 19.610              | 19.908 | 4.902  | 0.4510  | 2.939     |
| 9.615               | 4.988  | 2.404  | 0.7450  | 2.980     |
| 9.615               | 4.988  | 2.403  | 0.7235  | 3.003     |
| 41.840              | 17.365 | 11.510 | 0.7960  | 3.027     |
| 22.523              | 18.695 | 4.504  | 1.0075  | 3.058     |
| 42.017              | 17.439 | 10.504 | 1.130   | 3.158     |
| 9.634               | 4.998  | 1.927  | 1.217   | 3.171     |
| 24.663              | 18.611 | 4.484  | 1.349   | 3.175     |
| 42.192              | 17.512 | 9.493  | 1.629   | 3.284     |
| 26.786              | 18.528 | 4.464  | 1.771   | 3.289     |
| 28.889              | 18.446 | 4.444  | 2.300   | 3.394     |
| 74.630              | 15.100 | 18.660 | 2.000   | 3.416     |
| 42.372              | 17.586 | 8.474  | 2.367   | 3.411     |
| 30.973              | 18.364 | 4.425  | 2.961   | 3.487     |
| 42.553              | 17.661 | 7.447  | 3.520   | 3.522     |
| 33.040              | 18.284 | 4.405  | 3.771   | 3.573     |
| 75.760              | 15.330 | 15.150 | 5.650   | 3.795     |

Table 2. (Continued)

| Concentration (mM)                    |       |       |         |           |
|---------------------------------------|-------|-------|---------|-----------|
| $P_T$                                 | $H_T$ | Al    | F       | $\bar{n}$ |
| <u>In 0.3 M <math>NH_4NO_3</math></u> |       |       |         |           |
| 0.600                                 | 5.153 | 1.250 | 0.00040 | 0.478     |
| 1.000                                 | 5.153 | 1.250 | 0.00159 | 0.794     |
| 1.500                                 | 5.153 | 1.250 | 0.00268 | 1.190     |
| 1.470                                 | 2.940 | 1.220 | 0.00460 | 1.193     |
| 1.760                                 | 2.940 | 1.220 | 0.00870 | 1.420     |
| 2.050                                 | 2.940 | 1.220 | 0.01567 | 1.640     |
| 2.350                                 | 2.930 | 1.220 | 0.02720 | 1.856     |
| 2.500                                 | 5.153 | 1.250 | 0.03056 | 1.884     |
| 2.640                                 | 2.930 | 1.220 | 0.0481  | 2.042     |
| 3.000                                 | 5.153 | 1.250 | 0.0593  | 2.179     |
| 2.927                                 | 2.927 | 1.220 | 0.0812  | 2.196     |
| 3.216                                 | 2.923 | 1.218 | 0.1251  | 2.334     |
| 3.794                                 | 2.918 | 1.216 | 0.2397  | 2.560     |
| 4.369                                 | 2.913 | 1.214 | 0.396   | 2.726     |
| 5.000                                 | 5.153 | 1.250 | 0.388   | 2.765     |
| 4.942                                 | 2.907 | 1.211 | 0.598   | 2.846     |
| 5.760                                 | 4.320 | 1.200 | 0.713   | 2.955     |
| 6.000                                 | 5.153 | 1.250 | 0.626   | 2.986     |
| 5.797                                 | 2.899 | 1.208 | 0.958   | 3.002     |
| 8.570                                 | 4.290 | 1.190 | 2.033   | 3.302     |
| 10.000                                | 5.153 | 1.250 | 2.274   | 3.562     |
| 20.000                                | 5.153 | 2.500 | 6.064   | 3.844     |
| <u>In 0.1 M <math>NH_4NO_3</math></u> |       |       |         |           |
| 1.012                                 | 1.012 | 1.242 | 0.00089 | 0.813     |
| 1.214                                 | 1.214 | 1.242 | 0.00145 | 0.975     |
| 1.416                                 | 1.416 | 1.242 | 0.00275 | 1.135     |
| 1.618                                 | 1.618 | 1.242 | 0.00368 | 1.296     |
| 1.618                                 | 1.618 | 1.242 | 0.00401 | 1.295     |
| 1.820                                 | 1.820 | 1.242 | 0.00532 | 1.455     |
| 1.820                                 | 1.820 | 1.242 | 0.00574 | 1.453     |
| 2.022                                 | 2.022 | 1.241 | 0.00730 | 1.613     |
| 2.022                                 | 2.022 | 1.241 | 0.00827 | 1.610     |
| 2.022                                 | 2.022 | 1.241 | 0.01056 | 1.606     |
| 2.223                                 | 2.223 | 1.241 | 0.01230 | 1.762     |
| 2.223                                 | 2.223 | 1.241 | 0.01340 | 1.760     |
| 2.425                                 | 2.425 | 1.248 | 0.01950 | 1.895     |
| 2.425                                 | 2.425 | 1.241 | 0.02057 | 1.903     |

Table 2. (Continued)

| Concentration (mM) |        |       |         |           |
|--------------------|--------|-------|---------|-----------|
| $F_T$              | $H_T$  | Al    | F       | $\bar{n}$ |
| 1.015              | 1.015  | 0.498 | 0.02678 | 1.936     |
| 2.627              | 2.627  | 1.241 | 0.02787 | 2.044     |
| 2.828              | 2.828  | 1.240 | 0.04210 | 2.165     |
| 2.828              | 2.828  | 1.240 | 0.04996 | 2.144     |
| 3.029              | 3.029  | 1.240 | 0.06047 | 2.271     |
| 3.029              | 3.029  | 1.240 | 0.07455 | 2.232     |
| 3.231              | 3.231  | 1.240 | 0.08162 | 2.366     |
| 1.482              | 1.482  | 0.494 | 0.1250  | 2.450     |
| 3.634              | 3.634  | 1.239 | 0.1287  | 2.530     |
| 3.033              | 3.033  | 0.993 | 0.1568  | 2.526     |
| 4.036              | 4.036  | 1.239 | 0.1862  | 2.649     |
| 4.036              | 4.036  | 1.239 | 0.1934  | 2.627     |
| 2.028              | 2.028  | 0.498 | 0.2715  | 2.740     |
| 5.040              | 5.040  | 1.238 | 0.3226  | 2.909     |
| 4.040              | 4.040  | 0.992 | 0.3409  | 2.787     |
| 2.071              | 1.479  | 0.493 | 0.3350  | 2.837     |
| 6.041              | 6.041  | 1.236 | 0.4987  | 2.986     |
| 7.034              | 7.034  | 1.481 | 0.5231  | 2.893     |
| 6.041              | 6.041  | 1.236 | 0.5354  | 2.882     |
| 5.044              | 5.044  | 0.991 | 0.5354  | 2.912     |
| 3.017              | 3.017  | 0.497 | 0.5570  | 2.941     |
| 7.041              | 7.041  | 1.235 | 0.6952  | 2.961     |
| 6.048              | 6.048  | 0.990 | 0.7199  | 2.997     |
| 7.048              | 7.048  | 0.989 | 0.8952  | 3.055     |
| 10.019             | 10.019 | 1.476 | 0.9226  | 3.096     |
| 8.039              | 8.039  | 1.234 | 0.8111  | 3.124     |
| 10.029             | 10.029 | 1.231 | 1.105   | 3.191     |
| 12.012             | 12.012 | 1.229 | 1.374   | 3.240     |
| 13.986             | 13.986 | 1.227 | 1.618   | 3.288     |
| 15.953             | 15.953 | 1.224 | 1.847   | 3.324     |
| 19.844             | 19.844 | 1.462 | 2.039   | 3.308     |
| 18.108             | 18.108 | 1.222 | 2.084   | 3.351     |
| 19.863             | 19.863 | 1.219 | 2.279   | 3.338     |
| 21.807             | 21.807 | 1.217 | 2.474   | 3.349     |



Table 2. (Continued)

| Concentration (mM)                 |        |       |         |           |
|------------------------------------|--------|-------|---------|-----------|
| $F_T$                              | $H_T$  | Al    | F       | $\bar{n}$ |
| In 0.01 M $\text{NH}_4\text{NO}_3$ |        |       |         |           |
| 1.000                              | 5.153  | 2.500 | 0.00014 | 0.400     |
| 1.000                              | 5.153  | 1.250 | 0.00046 | 0.797     |
| 2.500                              | 5.153  | 2.500 | 0.00086 | 0.998     |
| 3.212                              | 3.212  | 2.711 | 0.00150 | 1.182     |
| 3.218                              | 3.218  | 2.223 | 0.00337 | 1.440     |
| 4.000                              | 5.153  | 2.500 | 0.00515 | 1.585     |
| 2.022                              | 2.022  | 1.241 | 0.00555 | 1.613     |
| 3.024                              | 3.024  | 1.733 | 0.00836 | 1.723     |
| 3.225                              | 3.225  | 1.732 | 0.01150 | 1.829     |
| 2.500                              | 5.153  | 1.250 | 0.01560 | 1.912     |
| 5.000                              | 5.153  | 2.500 | 0.01840 | 1.948     |
| 3.030                              | 3.030  | 1.240 | 0.0581  | 2.237     |
| 3.030                              | 3.030  | 1.240 | 0.0550  | 2.247     |
| 4.036                              | 4.036  | 1.239 | 0.1682  | 2.572     |
| 7.500                              | 5.153  | 2.500 | 0.1598  | 2.603     |
| 5.040                              | 5.040  | 1.238 | 0.2968  | 2.756     |
| 5.000                              | 5.153  | 1.250 | 0.2600  | 2.807     |
| 6.041                              | 6.041  | 1.236 | 0.4247  | 2.884     |
| 7.041                              | 7.041  | 1.235 | 0.5579  | 2.948     |
| 8.039                              | 8.039  | 1.234 | 0.6795  | 3.015     |
| 10.000                             | 5.153  | 2.500 | 0.496   | 3.028     |
| 10.029                             | 10.029 | 1.232 | 0.908   | 3.120     |
| 12.011                             | 12.011 | 1.229 | 1.132   | 3.163     |
| 13.896                             | 13.896 | 1.227 | 1.344   | 3.156     |
| 15.952                             | 15.952 | 1.224 | 1.517   | 3.273     |
| 17.912                             | 17.912 | 1.222 | 1.711   | 3.262     |
| 19.863                             | 19.863 | 1.219 | 1.887   | 3.271     |
| 23.743                             | 23.743 | 1.215 | 2.2043  | 3.306     |
| 27.593                             | 27.593 | 1.210 | 2.486   | 3.352     |
| 38.966                             | 38.966 | 1.196 | 3.240   | 3.362     |

Table 3. Stability Quotients of Hydrogen-Fluoride System  
in  $\text{NH}_4\text{NO}_3$  at  $25^\circ\text{C}$

| <u>Ionic Strength,</u><br><u>M</u> | <u><math>k_1</math></u> | <u><math>k_2</math></u> |
|------------------------------------|-------------------------|-------------------------|
| 0.53[8]                            | 658                     | 3.9                     |
| 0.5                                | 692                     | 5.0                     |
| 0.3                                | 742                     | 3.7                     |
| 0.1                                | 878                     | 6.8                     |
| 0.01                               | 1203                    | 5.8                     |

[8] C. Brosset, Svensk Kem. Tidskr. 54, 155 (1942).

Table 4. Stability Quotients of Aluminum-Fluoride System  
in  $\text{NH}_4\text{NO}_3$  at  $25^\circ\text{C}$

| Ionic Strength,<br>M | $k_1$              | $k_2$              | $k_3$              | $k_4$              |
|----------------------|--------------------|--------------------|--------------------|--------------------|
| 0.53[5]              | $1.36 \times 10^6$ | $1.04 \times 10^5$ | $7.16 \times 10^3$ | $5.50 \times 10^2$ |
| 0.5                  | $1.21 \times 10^6$ | $8.53 \times 10^4$ | $4.85 \times 10^3$ | $3.18 \times 10^2$ |
| 0.3                  | $1.96 \times 10^6$ | $9.38 \times 10^4$ | $5.32 \times 10^3$ | $3.15 \times 10^2$ |
| 0.1                  | $2.49 \times 10^6$ | $1.56 \times 10^5$ | $8.10 \times 10^3$ | $2.66 \times 10^2$ |
| 0.01                 | $4.47 \times 10^6$ | $2.73 \times 10^5$ | $8.41 \times 10^3$ | $2.38 \times 10^2$ |

Table 5. Stability Constants of Hydrogen-Fluoride System

|                    | This Work                              |          | Reference [4] |
|--------------------|--|----------|---------------|
|                    | <u>log K <math>\pm 2\sigma</math>*</u> | <u>C</u> |               |
| log K <sub>1</sub> | 3.164 $\pm$ 0.010                      | -0.05    | 3.17          |
| log K <sub>2</sub> | 0.7 $\pm$ 0.2                          | 0        | 0.59          |

\* $\sigma$  is standard deviation of K<sub>n</sub>, calculated from the four K<sub>n</sub> values used in the extrapolation

Table 6. Stability Constants of Aluminum-Fluoride System

|                    | This Work                              |          | References [5,9] |
|--------------------|--|----------|------------------|
|                    | <u>log K <math>\pm 2\sigma</math>*</u> | <u>C</u> |                  |
| log K <sub>1</sub> | 6.98 $\pm$ 0.16                        | -0.4     | 7.00             |
| log K <sub>2</sub> | 5.62 $\pm$ 0.04                        | 0        | 5.55             |
| log K <sub>3</sub> | 4.05 $\pm$ 0.10                        | 0        | 4.23             |
| log K <sub>4</sub> | 2.38 $\pm$ 0.02                        | -0.2     | 2.74             |

\*See footnote, Table V.

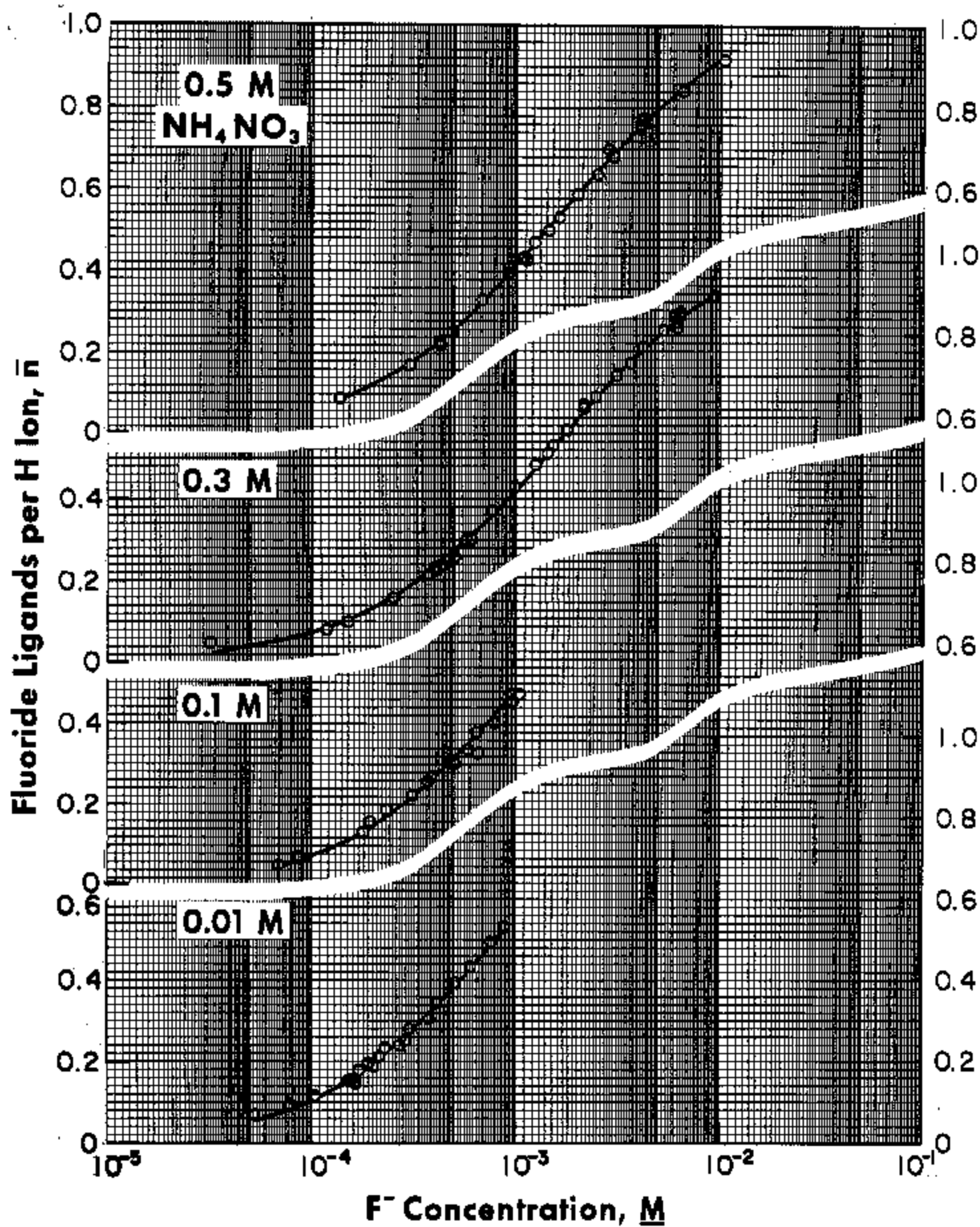


Fig. 1. Hydrogen-Fluoride System in  $\text{NH}_4\text{NO}_3$ .

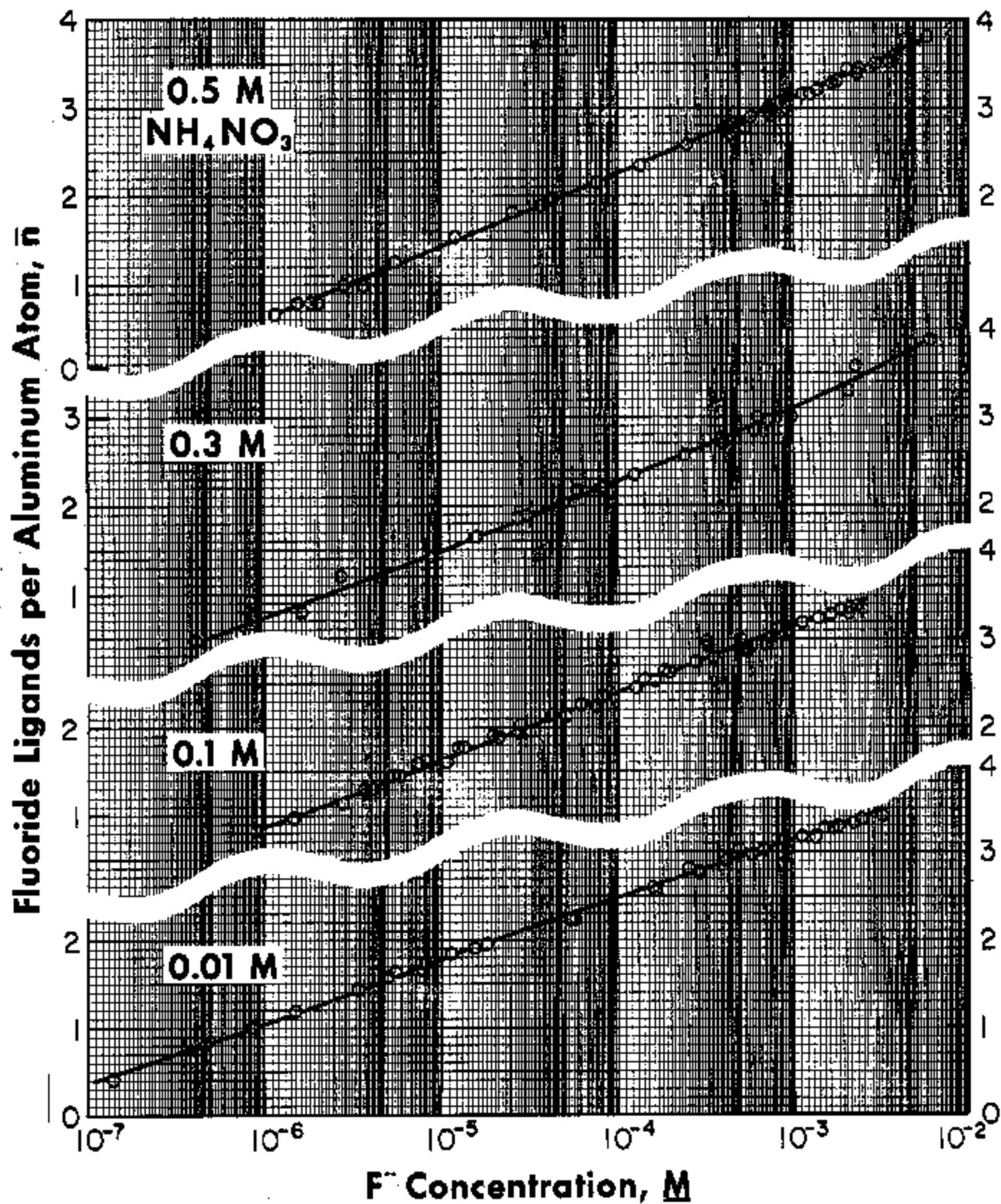


Fig. 2. Aluminum-Fluoride System in  $\text{NH}_4\text{NO}_3$ .